



1

$$\textcircled{F} \quad \phi(\{x:D \cdot P_x\}) = 0 \Rightarrow \phi(\text{IF } \langle x:D \rightarrow P_x \rangle D \text{ THEN } D \text{ ELSE NULL}) = 0$$

$$\Rightarrow D \not\Rightarrow P_x \Rightarrow \exists (x:D \cdot P_x) = \perp \Rightarrow \neg(\exists x:D \cdot P_x)$$

$$\textcircled{P} \quad \phi(\{x:D \cdot P_x\}) = 1$$

$$\Rightarrow \exists x:D \cdot P_x \wedge \forall x,y:D \cdot P_x \wedge P_y \rightarrow x=y$$

$$\textcircled{E} \quad \phi(\{x:D \cdot P_x\}) = 2$$

$$\Rightarrow \exists x:D \cdot P_x \wedge \neg(\exists x,y,z:D \cdot x \neq y \wedge x \neq z \wedge y \neq z \wedge P_x \wedge P_y \wedge P_z)$$

2

$$\underline{\exists}: \quad \exists x:D \cdot P_x \Rightarrow \phi(\{x:D \cdot P_x\}) \geq 1$$

$$\underline{\forall}: \quad \forall x:D \cdot P_x \Rightarrow \phi(\{x:D \cdot P_x\}) = |D|$$