Ultra-Wideband Waveform Generation Using Nonlinear Propagation in Optical Fibers

Avi Zadok\textsuperscript{1}, Daniel Grodensky\textsuperscript{1}, Daniel Kravitz\textsuperscript{1}, Yair Peled\textsuperscript{2}, Moshe Tur\textsuperscript{2}, Xiaoxia Wu\textsuperscript{3} and Alan E. Willner\textsuperscript{3}

\textsuperscript{1}Bar-Ilan University
\textsuperscript{2}Tel-Aviv University
\textsuperscript{3}University of Southern California

1,2Israel
3USA

1. Introduction

Ultra-wideband (UWB) radio is a transmission technology that is based on short pulses, whose spectral width is on the order of several GHz. UWB signals are free of sine-wave carriers, and their duty cycle and power spectral density are low. These characteristics provide UWB radio with unique advantages: improved immunity to multi-path fading, increased ranging resolution, large tolerance to interfering legacy systems, enhanced ability for penetrating obstacles, and low electronic processing complexity at the receiver. UWB technology is considered attractive for a myriad of applications, including high-speed internet access, sensor networks, high accuracy localization, precision navigation, covert communication links, ground-penetrating radar, and through-the-wall imaging (Yang & Giannakis, 2004).

Of the various potential UWB radio applications, much attention has turned to wireless personal area networks, which address short-range, ad-hoc, and high-rate connectivity among portable electronic devices. UWB radio is among the standards that are being considered to replace cables in such networks, due to its multi-path and interference tolerance, low power, and high efficiency. Research efforts in this area have intensified since 2002 when the United States Federal Communication Commission (FCC) allocated the frequency range of 3.6-10.1 GHz for unlicensed, UWB indoor wireless communication (Federal Communications Commission [FCC], 2002). Interest is not limited to indoor wireless communication only: the FCC report relates to imaging systems and vehicular radar systems as well (FCC, 2002). The vehicular radar standard, in particular, specifies a high central frequency of 24 GHz or higher (FCC, 2002). The electronic generation of complex UWB waveforms at such high frequencies is increasingly challenging.

The FCC standard imposes several limitations on the transmitted signals. First, the power spectral density must comply with complicated spectral masks (FCC, 2002). In addition, the total signal power is severely restricted, limiting the range of UWB indoor wireless transmission, for example, to only 10-15 m. In many scenarios, UWB radio-based systems would need to extend their wireless transmission range by other distribution means. As the
frequencies of UWB signals continue to increase, with 100 GHz transmission already reported (Chow et al., 2010), optical fibers become the preferable distribution medium. With radio-over-fiber integration on the horizon, the generation of the UWB pulses by photonic methods becomes attractive. Microwave-photonic generation techniques can offer flexible tuning of high-frequency pulse shapes, inherent immunity to electromagnetic interference, and parallel processing via wavelength division multiplexing (Capmany et al., 2005). Driven by the promises of integration and flexibility, much research effort has been dedicated to photonic generation of UWB waveforms in recent years.

Most microwave-photonic UWB generation schemes thus far target *impulse radio* implementations: the transmission of tailored short pulses and their subsequent coherent detection. One category of photonic UWB generation techniques relied on the conversion of phase to intensity modulation (Yao et al., 2007; Zeng & Yao, 2006; Zeng et al., 2007). This method is simple to implement, however it offers few degrees of freedom for pulse shaping and minimal reconfiguration. Waveforms generated using this method are restricted to a Gaussian mono-cycle or a Gaussian doublet shape. Higher-order pulse shapes were generated based on microwave-photonic tapped delay line filters, with both positive and negative coefficients (Bolea et al., 2009; Bolea et al., 2010). Pulse generation based on four-coefficient filters had been demonstrated (Bolea et al., 2009), however each additional coefficient required an extra laser source.

Another interesting approach is based on nonlinear dynamics in semiconductor optical amplifiers (SOAs) and laser diodes. Cross-gain modulation (XGM) effects in SOAs and cross-absorption effects in electro-absorption modulators had been used in Gaussian monocycle and doublet waveform generation (Ben-Ezra et al., 2009; Wu, et al., 2010; Xu et al., 2007a, 2007b). Relaxation oscillations in directly-modulated or externally-injected distributed feedback lasers were recently demonstrated as well (Gibbon et al., 2010; Pham et al., 2011; Yu et al., 2009). The technique is well suited to the FCC spectral mask for indoor wireless communication: wireless transmission of 3.125 Gbits/s, employing high-order waveforms, had been experimentally demonstrated (Gibbon et al., 2010; Pham et al., 2011). On the other hand, waveform generation based on relaxation oscillations is restricted to the order of 10 GHz by the laser diode dynamics.

The most elaborate waveform tailoring was provided by optical spectrum shaping and subsequent frequency-to-time mapping (Abtahi et al., 2008a, 2008b, 2008c; McKinney et al., 2006; McKinney, 2010). These techniques relied on careful spectral shaping of the transmitted waveforms in order to maximize the transmitted power within the constraints of the FCC mask. However, the demonstrations required mode-locked laser sources, and either bulky free-space optics (McKinney et al., 2006; McKinney, 2010) or highly complex fiber gratings with limited tuning (Abtahi et al., 2008a, 2008b, 2008c). Major progress had been recently achieved, with the pulse-shaping optics successfully replaced by a programmable, integrated silicon-photonic waveguide circuit (Khan et al., 2010).

Nonlinear propagation effects in optical fibers are powerful tools for optical signal processing. However, they have been seldom used in UWB pulse generation research. Li and coauthors used cross-gain modulation in an optical parametric amplifier to generate monocycle and doublet pulse shapes (Li et al., 2009). Velanas and coauthors used a cross-phase-modulation (XPM) based technique to obtain monocycle shapes (Valenas et al., 2008). Both schemes required two input laser sources.

In the first section of this work, we use nonlinear propagation of a pulse train from a single laser source for the generation of high-order UWB impulse radio waveforms (Zadok et al.,
ultra-wideband waveform generation using nonlinear propagation in optical fibers

2009; zadok et al., 2010a, 2010b, ©2010 IEEE). All-optical edge detectors of the input pulses intensity are used to generate two temporally-narrowed replicas of the input pulse train. The edge detection relies on the time-varying chirp introduced by self-phase modulation (SPM), and judiciously tuned optical filters. SPM accumulates through propagation along sections of fiber, which can also serve for the distribution of pulses from a network terminal to a remote antenna element. The shapes of the narrowed replicas are subtracted from that of the original pulse train in a broadband, balanced differential detector. The resulting waveforms are highly reconfigurable through adjustments of the input power and tuning of the optical filters. High-order UWB waveforms, having a center frequency of 34 GHz and a fractional bandwidth of 70% are generated.

UWB architectures that are based on impulse radio require elaborate pulse shaping and a detailed knowledge of the communication channel properties (qiu et al., 2005; yang & Giannakis 2004). A possible alternative is the transmission of modulated, broadband noise waveforms. One such implementation relies on direct energy detection (sahin et al., 2005). Incoherent detection, however, compromises the immunity to interference of UWB technology. Coherent detection can be restored using transmit-reference (TR) schemes, in which the modulated noise is accompanied by a delayed, unmodulated replica of itself (narayanan & chuang, 2007). Data is recovered by a matched delay at the receiver end (narayanan & chuang, 2007), and knowledge of the channel response is not required (sahin et al., 2005). Photonic generation of UWB noise has been demonstrated recently, based on the chaotic dynamics of a laser diode in a feedback loop (zheng et al., 2010).

In the second part of this work we propose, analyze and demonstrate the photonic generation of UWB noise, based on the amplified spontaneous emission associated with stimulated Brillouin scattering in optical fibers (SBS-ASE) (peled et al., 2010, ©2010 IEEE). The noise bandwidth is extended to 1.1 GHz, using a recently proposed method for broadening of the SBS process (zadok et al., 2007). Gaussian noise of such bandwidth can be readily generated electrically, however photonic generation techniques are appealing from a radio-over-fiber integration standpoint (yao et al., 2007). Both direct detection and TR-assisted coherent detection are demonstrated. The performance is in agreement with the theoretical analysis.

Finally, as noted above, UWB waveforms find applications in various radar systems. Noise-based waveforms, in particular, provide better immunity to interception and jamming (chuang et al., 2008; narayanan, 2008). Similarly to UWB communication, photonic techniques could provide flexible and reconfigurable generation of broadband, high-carrier frequency noise waveforms, integrated with simple long-reach distribution. In the last section of this work, we show preliminary ranging measurements of metal objects based on SBS-ASE noise waveforms.

2. UWB impulse radio generation using self-phase modulation in optical fibers

2.1 Self-phase modulation based edge detection

Consider the optical field \( E_{in}(t) \) of an input train of super-Gaussian pulses (zadok et al., 2010b, ©2010 IEEE):

\[
E_{in}(t) = \sum_n \sqrt{P_n} \exp \left[ -\left( \frac{|t - nT_i|}{2\tau_0} \right)^n \right] \exp(j\omega_0 t), \tag{1}
\]
with a peak power level $P_\text{in}$, central optical frequency $\omega_0$, width parameter $\tau_0$ and pulse separation $T_0$. The parameter $m$ determines the exact shape of the input pulses, and $t$ denotes time. In propagating along a highly nonlinear fiber (HNLF) of length $L$ [km] and negligible dispersion, the optical field undergoes SPM:

$$E_{\text{HNLF}}(t) = E_\text{in}(t) \exp[j\varphi(t)] = E_\text{in}(t) \exp[jyL|E_\text{in}(t)|^2]$$  \hspace{1cm} (2)

where $\gamma$ [W · km]$^{-1}$ is the nonlinear coefficient of the fiber. The nonlinearly induced phase modulation $\varphi(t)$ represents an effective temporally-varying shift of the optical frequency (chirp):

$$\Delta f_{\text{pulse}}(t) = \frac{1}{2\pi} \frac{d\varphi(t)}{dt} = \frac{\gamma L}{2\pi} \frac{|E_\text{in}(t)|^2}{dt}$$  \hspace{1cm} (3)

Figure 1 shows the instantaneous power $|E_\text{in}(t)|^2$ of a single input super-Gaussian pulse with $m = 5$ (top panel), and the corresponding $\Delta f_{\text{pulse}}(t)$ for a 1 km-long HNLF with $\gamma = 11.3$ [W · km]$^{-1}$ (bottom panel). The leading (trailing) edge of the pulse is associated with a positive (negative) frequency shift. Edge detection of $E_{\text{HNLF}}(t)$ is implemented by an optical bandpass filter (BPF) of spectral width $2\delta$, detuned from $\omega_0$ by a frequency offset $\Delta\omega > \delta > 0$. The BPF would block most of the waveform, except for a segment of sufficient SPM: $2\pi \cdot \Delta f_{\text{pulse}}(t) > \Delta\omega - \delta$. As seen in equation (3), this segment corresponds to the leading edge of the pulse. The BPF therefore represents an all-optical intensity edge detector. The details of the narrowed replica of the pulse at the BPF output are determined by its spectral width and detuning as well as the input power $P_\text{in}$. The endpoints of the filtered waveform $t_{1,2}$ are approximately given by: $d[E_\text{in}(t_{1,2})]^2/dt = (\Delta\omega - \delta)/\gamma L$. The trailing edge can be filtered in a similar manner, with $\Delta\omega < 0$, $|\Delta\omega| > \delta > 0$. Figure 2 shows the instantaneous power $|E(t)|^2$ at the output of two 75 GHz-wide BPFs, whose central frequencies are detuned from $\omega_0$ by $\Delta\omega_2/2\pi = \pm 135$ GHz, respectively. As expected, the filtered waveforms emphasize the pulse edges, and both are narrower than the original input pulse. The shape of the two narrowed replicas can be subtracted from that of the original pulse to generate an UWB waveform, as described next.

### 2.2 UWB waveform generation using all-optical edge detectors

Figure 3 shows a schematic drawing of a setup for UWB waveform generation, based on all-optical edge detection (Zadok et al., 2010b, ©2010 IEEE). The input super-Gaussian pulse train is split in two branches. The upper branch includes a high-power erbium-doped fiber amplifier (EDFA) and an HNLF section. At the HNLF output, the spectrally broadened pulses are split into two paths once again, and the light in each path is filtered by an individually tunable BPF: one is tuned to detect the pulse leading edge as discussed above, whereas the other is adjusted as a trailing edge detector. The power level of each of the two pulse train replicas is individually adjusted by a variable optical attenuator (VOA). In addition, the relative delay between the two pulse trains can be modified by a tunable delay line (TDL). The two pulse trains are then joined together and directed to the negative port of a balanced, differential detector. Since the difference between the central frequencies of the two replicas is outside the detector bandwidth, beating between the two is largely avoided.
A reference pulse train, arriving from the lower branch of the setup, is detected at the positive port of the balanced detector. The relative delay and magnitude of the reference pulse train are controlled by a second EDFA and TDL.

Fig. 1. Top - instantaneous power of an input super-Gaussian pulse: $m = 5$, $\tau_\alpha = 27$ ps, $P_i = 1.7$ W. Bottom - simulated SPM-induced instantaneous frequency shift $\Delta f_{\text{pulse}}(t): L = 1$ km, $\gamma = 11.3$ [W·km]$^{-1}$. Horizontal shaded regions in the bottom panel schematically denote the passbands of two detuned optical filters. Vertical dashed lines schematically illustrate the temporal edges of the corresponding waveforms at the filters output. ©2010 IEEE.

Fig. 2. Solid - instantaneous power of an input super-Gaussian pulse (same as top panel of Fig. 1). Dashed - simulated instantaneous pulse power following propagation in a HNLF and filtering by a 75 GHz-wide BPF, detuned from $\omega_s$ by $\Delta \omega_s / 2\pi = 135$ GHz. HNLF parameters are the as those in the bottom panel of Fig. 1. Dashed-dotted - same as dashed curve, with the BPF detuned from $\omega_s$ by $\Delta \omega_s / 2\pi = -135$ GHz. ©2010 IEEE.
The electrical waveform at the balanced detector output can be expressed as:

\[ V(t) \propto E_w(t) - a_\pm E_{t-}(t-t_\pm) - a_\pm E_{t+}(t-t_\pm) \]  \( (4) \)

where \( a_\pm \) and \( t_\pm \) are the relative power levels and delays of the leading and trailing edge waveforms, respectively. Unless corrected by the TDLs, the relative delays \( t_\pm \) correspond to \( \max(\min) \) of the input intensity derivative. The complete waveform design requires a numeric calculation. Nonetheless, the following relations may serve as useful starting points:

\[ t_\pm \approx -\tau_\pm, \quad a_\pm \approx \frac{1}{2} \int E_w(t) dt / \int E_r(t) dt \]

The central frequency \( f_c \) of \( V(t) \) is on the order of \( 1/(t_2 - t_1) \), where \( |t_2 - t_1| \) is the temporal width of the narrowed replica at the output of the edge detectors (see previous section).

Figure 4 shows a simulated example of the normalized shape of \( V(t) \) (top panel) and its corresponding power spectral density \( |V(\Omega)|^2 \) (bottom), where \( \Omega \) represents a radio frequency (RF) variable. The calculation parameters were the same as those of the previous section, with \( a_\pm = 1.85 \) and \( t_\pm = \pm 10 \) ps. The central frequency \( f_c \) of the high-order, UWB output waveform is 34 GHz. The high and low -10 dB cutoff frequencies \( f_{HL} \) are 47 GHz and 23 GHz, respectively, providing a fractional bandwidth \( B_r = (f_{HL} - f_c) / f_c \) of 70%. \( V(t) \) can be simply modified through changing the peak power, width and shape of the incoming pulse train, the detuning of the BPFs, and the relative magnitude and delay of the replica trains of narrowed pulses. Experimental generation of UWB waveform is described next.
Ultra-Wideband Waveform Generation Using Nonlinear Propagation in Optical Fibers

Fig. 4. Top – Simulated output waveform $V(t)$. The input pulse, HNLF and BPFs parameters are the same as those of Figs. 1 and 2, $a_z = 1.85$ and $t_z = \pm 10$ ps. Bottom – the corresponding RF spectrum $|\tilde{V}(\Omega)|^2$. ©2010 IEEE.

2.3 Experimental results

The generation of UWB pulses was demonstrated experimentally, using the setup of Fig. 3 (Zadok et al., 2010b, ©2010 IEEE). The parameters of the input pulse train and HNLF, and the settings of the BPFs, VOAs and TDLs were the same as those of the previous sections. The separation $T_o$ between neighboring pulses was 600 ps, corresponding to a data rate of 1.67 Gb/s. The average power of the amplified, input pulse train was 160 mW. Figure 5 shows the measured optical spectra $|E_a(\lambda)|^2$, $|E_{\text{HNLF}}(\lambda)|^2$ and $|E_{\text{NL}}(\lambda)|^2$, corresponding to $E_a(t)$, $E_{\text{HNLF}}(t)$ and $E_{\text{NL}}(t)$ respectively, as a function of wavelength $\lambda$.

Figure 6 (top) shows the measured $V(t)$ alongside the corresponding simulation. The experimental RF spectrum $|\tilde{V}(\Omega)|^2$, calculated by taking the Fourier transform of the measured $V(t)$, is shown at the bottom of Fig. 6 alongside the simulated results. The experimental waveform generally agrees with the simulation.

The flexibility of the waveform generation method is illustrated in Fig. 7 (Zadok et al., 2009; Zadok et al., 2010a), in which the setup parameters were adjusted to approximate the FCC mask for unlicensed indoor wireless UWB communication (FCC, 2002). In this experiment, Gaussian pulses ($m = 2$) of width $\tau_o = 100$ ps, peak power $P_{\text{in}} = 1$ W and spacing $T_o = 800$ ps were used. Only a single edge detection BPF was used in the experiment, with a spectral width of 40 GHz and detuning $\Delta\omega/2\pi$ of 30 GHz. The normalized output waveform $V(t)$ approximates a Gaussian doublet pulse shape (top panel). The calculated $|\tilde{V}(\Omega)|^2$ is drawn
on the lower panel, alongside the FCC mask. The measurement generally complies with the mask requirements, although infringements can be seen at the lower frequency range.

Fig. 5. Measured optical power spectra corresponding to $E_{\text{on}}(t)$ (dashed, black), $E_{\text{HNLF}}(t)$ (dotted, blue), $E(t)$ (solid, magenta) and $E_{\text{off}}(t)$ (dashed-dotted, red). The experimental parameters were the same as those of the simulations in Fig. 4. ©2010 IEEE.

The FCC mask infringements of the experimental Fig. 7 can be considerably reduced with the use of a narrower BPF: Figure 8 shows an example of simulated $V(t)$ and $|\tilde{V}(\Omega)|$ obtained with a single 10-GHz wide BPF. Results may be further improved by using two BPFs, as in Fig. 6.

2.4 Discussion and future work

The proposed technique for the photonic generation of UWB relies on all-optical detection of intensity edges of incoming super-Gaussian pulses. The technique could be particularly suitable for high-frequency waveforms, such as those intended for high-resolution vehicular radar systems. The edge detectors were implemented based on SPM in a section of HNLF, and using two BPFs in parallel. However, both edges might be detected simultaneously with the application of just one band-stop optical filter centered at $\omega_c$, which would remove the center of the pulse (see Fig. 1). Data can be transmitted through simple on-off keying of the input pulses. On the other hand, pulse polarity modulation is not simply supported by the proposed approach.

The waveform generation setup includes multiple optical paths, the lengths of which were not matched in the experiment. The integrity of the UWB shape in a data-carrying, operational system could require path length equalization on mm scale. The problem might
be alleviated by using short fiber spans and high peak power levels, environmental isolation of fiber sections or active compensation. Alternatively, the relative delays $t_i$ could be controlled using dispersion rather than TDLs along different paths. The stability of the experimental setup was thus far validated over a couple of hours. Long term stability was not tested. The transmission of actual data using the proposed approach is the subject of further work.

![Graph](image.png)

**Fig. 6.** Top – Simulated (solid, blue) and measured (dashed, red) output waveform $V(t)$.

The experimental parameters were the same as those of the simulations in Fig. 4. Bottom – the corresponding simulated (solid, blue) and calculated experimental (dashed, red) RF spectra $|V(\Omega)|^2$. ©2010 IEEE.

The shaping and distribution scheme of the UWB pulses requires a two-fiber connection between a transmitter and a remote antenna element. Single-fiber transmission would be possible if a reference pulse shape $|E_{\text{ref}}(t)|^2$ could be extracted from the SPM-broadened $E_{\text{NLFE}}(t)$ at the receiver. Ideally $|E_{\text{NLFE}}(t)|^2 = |E_{\text{ref}}(t)|^2$, however residual dispersion and EDFA noise might distort the reference pulse shape. A potential solution might be narrow-band optical filtering centered at $\omega_0$. The comparison of the technique proposed in this work to previous approaches draws interesting analogies. Here, SPM introduces a time-to-frequency mapping, in which different temporal sections of the input pulses acquire different frequency shifts. This process is somewhat analogous to frequency-to-time mapping-based techniques (Abtahi et al., 2008a; McKinney et al., 2006; Wang et al., 2007), in which dispersion is used to assign a different delay to different spectral components of an input waveform. The subtraction of
the intensity profile of delayed replicas from the original pulse shape might be viewed as a tapped-delay line filtering method. It should be noted, though, that the subtracted waveforms are obtained through nonlinear processing and are not scaled copies of the input. The nonlinear propagation enables the generation of higher-order waveforms while using only two replicas, and also allows for simple reconfiguration through input power adjustments.

Fig. 7. Top– measured $V(t)$. Bottom– calculated experimental RF power spectrum $|V(\Omega)|^2$ (solid), alongside the FCC mask for indoor UWB communication (FCC, 2002) (dashed). Input parameters: $P_in = 1 \text{ W}$, $\tau_p = 100 \text{ ps}$, $m = 2$, $\tau_s = 800 \text{ ps}$. HNLF parameters: $L = 1 \text{ km}$, $\gamma = 11.3 \text{ [W km]^{-1}}$. A single 40-GHz wide BPF was used, detuned by $\Delta\omega/2\pi = 30 \text{ GHz}$. ©2010 IEEE.

3. UWB noise waveforms generation using stimulated Brillouin scattering amplified spontaneous emission

As discussed above, impulse radio UWB communication requires elaborate pulse shaping, using either electrical or optical means. Alternatively, the criteria of UWB transmission may be met based on modulated noise waveforms, which could be simpler to generate. UWB noise communication had been previously proposed and demonstrated in several works (Haartsen et al., 2004; Haartsen et al., 2005; Narayanan & Chuang, 2007; Sahin et al., 2005). However, only few studies examined the use of optical techniques for noise generation. In one such recent example (Zheng et al., 2010), UWB noise was generated based on the chaotic dynamics of a laser diode within a fiber-optic feedback loop. UWB noise can be readily generated using electrical techniques (Upadhyaya, 1999), however optical methods are nonetheless appealing as part of a radio-over-fiber integrated system.
The rejection of interfering signals in UWB receivers relies on a proper matched filtering of incoming waveforms. The matched filter, in turn, requires precise knowledge of the transmitted pulse shapes and the transfer properties of the communication channel. In noise-based UWB schemes, a reference waveform must be provided to the receiver separately. In such transmit-reference (TR) techniques, an unmodulated replica of the data-carrying noise waveform is transmitted in parallel. Data and reference can by time-multiplexed, or launched at different intermediate frequencies or over two orthogonal polarizations (Narayanan and Chuang, 2007). TR UWB communication based on optically generated waveforms is demonstrated below.

3.1 Broadband noise generation

Stimulated Brillouin scattering (SBS) requires the lowest activation power of all non-linear effects in silica optical fibers. In SBS, a strong pump wave and a typically weak, counter-propagating signal wave optically interfere to generate, through electrostriction, a traveling longitudinal acoustic wave. The acoustic wave, in turn, couples these optical waves to each other (Boyd, 2008). The SBS interaction is efficient only when the difference between the optical frequencies of the pump and signal waves is very close (within a few tens of MHz) to a fiber-dependent parameter, the Brillouin shift $\Omega_B$, which is of the order of $2\pi\cdot11$ GHz in silica fibers at room temperature and at 1550 nm wavelength (Boyd, 2008). An input signal
whose frequency is $\Omega_s$ lower than that of the pump, ('Stokes wave'), experiences SBS amplification. Among its numerous applications, SBS is used in optical processing of high frequency microwave signals (Loayssa et al., 2000; Loayssa & Lahoz, 2006; Loayssa et al., 2006; Shen et al., 2005; Zadok et al., 2007).

In the absence of a seed input signal wave, SBS could still be initiated by thermally-excited acoustic vibrations (Boyd, 2008). The naturally occurring vibrations scatter a fraction of the incident pump into a preliminary signal, which is then further amplified. In this scenario, SBS acts as a generator of amplified spontaneous emission (ASE) at the signal frequency. This SBS-ASE is the underlying mechanism of the UWB noise waveform generation described below. UWB generation requires a substantial spectral broadening of the inherently narrowband SBS process. Bandwidths of several GHz are routinely achieved through pump wave modulation (Zadok et al., 2007; Zhu et al., 2007).

A schematic drawing of a TR-assisted, SBS-ASE UWB noise transmitter is shown in Fig. 9 (Peled et al., 2010, ©2010 IEEE). Light from a distributed feedback (DFB) laser source is directly modulated and amplified. The spectrally broadened light is launched into a section of HNLF of length $L$ and loss coefficient $\alpha$ as an SBS pump. Let us denote the generated, counter-propagating SBS-ASE noise field as $E_s(t)$. The power spectral density (PSD) of $E_s(t)$ is given by (Wang et al., 1996):

$$P(\omega_s) \propto \#\omega_s \left[ \exp \left( g(\omega_s) L_{\text{eff}} - \alpha L \right) - 1 \right] \left[ 1 - \exp \left( -\alpha L \right) \right] \left[ \exp \left( g(\omega_s) L_{\text{eff}} \right) - 1 \right] \sqrt{g(\omega_s) L_{\text{eff}}}]$$

In (5) $L_{\text{eff}}$ is the effective length of the fiber, and $\omega_s$ is the optical frequency of the generated Stokes wave. For a broadened pump, the SBS power gain coefficient $g(\omega_s)$, in units of m$^{-1}$, can be approximated as (Zadok et al., 2007; Zhu et al., 2007):

$$g(\omega_s) \propto P_p(\omega_s + \Omega_s)$$

where $P_p$ denotes the pump PSD.

Careful synthesis of the pump laser direct modulation could provide a uniform $P_p$, and hence a uniform $P(\omega_s)$, within a range of several GHz (Zadok et al., 2007). The optical noise can be down-converted to the radio frequency (RF) domain through heterodyne beating with a local oscillator of frequency $\omega_{\text{lo}}$ on a broadband detector. The real-valued beating term $V(t)$ is proportional to a single ASE quadrature component, and is therefore of Gaussian statistics. Its PSD $\tilde{V}(\Omega)$ scales with $P(\omega_s = \Omega + \omega_{\text{lo}})$. The spectral width of $\tilde{V}(\Omega)$ is bounded by that of the pump.

### 3.2 Performance of transmit-reference UWB communication using SBS-ASE noise waveforms

In a TR-based implementation, the SBS-ASE noise field passes through an imbalanced Mach-Zehnder interferometer (MZI), with a differential delay of $\tau$ (see Fig. 9) (Peled et al., 2010, ©2010 IEEE). Light in the upper arm of the MZI is on/off modulated by information pulses of duration $T_\tau$. Following heterodyne down conversion, the electric signal to be transmitted can be expressed as:
Ultra-Wideband Waveform Generation Using Nonlinear Propagation in Optical Fibers

\[ V_{tx}(t) = \sum_{n} a_n \text{win}\left[\left(t-nT_o\right)/T_o\right]V(t) + V(t - \tau), \]  

(7)

where \( \text{win}(\xi) = 1 \) for \( 0 < \xi \leq 1 \) and equals zero elsewhere, \( n \) is an integer and \( a_n \) is a binary data value. Data is recovered at the receiver by electrically mixing the incoming signal with a replica that is delayed by \( \tau \), and integrating over \( T_o \):

\[ Y[n] = \int_{nT_o}^{(n+1)T_o} V_{tx}(t)V_{tx}(t + \tau)dt. \]

(8)

We require that \( \tau \ll T_o \), in which case the decision variables for ‘1’ and ‘0’ are expressed as:

\[ Y[0][n] = C_{V,\lambda,0}(0) + C_{V,\lambda,0}(\tau) + C_{V,\lambda,0}(-\tau) + C_{V,\lambda,0}(2\tau). \]

(9)

\[ Y[0][n] = C_{V,\lambda,0}(\tau) \]

(10)

where \( C_{V,\lambda,0}(\xi) = \int_{-\infty}^{\infty} V(t)V(t + \xi)dt \). Note that for \( \tau \ll T_o \), \( C_{V,\lambda,0}(\tau) \approx C_{V,\lambda,0}(-\tau) \). The ensemble averages of (9)-(10) are given by (Goodman, 2000):

\[ I_1 = \langle Y[0][n] \rangle_n = T_o\left[\Gamma_{\lambda}(0) + 2\Gamma_{\lambda}(\tau) + \Gamma_{\lambda}(2\tau)\right] \approx T_o\Gamma_{\lambda}(0). \]

(11)

\[ I_0 = \langle Y[0][n] \rangle_n = T_o\Gamma_{\lambda}(\tau) \ll I_1 \]

(12)

where \( \Gamma_{\lambda}(\xi) \) denotes the autocorrelation \( \langle V(t)V(t + \xi) \rangle \). Equation (12) requires that \( \tau \) is much longer than the coherence time \( \tau_c \) of \( V(t) \). Next the standard deviations \( \sigma_{1,0} \) of equations (9)-(10) are estimated. Using the high-order moment theorem for real variables of Gaussian statistics (Goodman, 2000):

\[ \sigma_{V,\lambda,0}^2(\xi) = \left( C_{V,\lambda,0}^2(\xi) \right)_n - \left( C_{V,\lambda,0}(\xi) \right)_n^2 \]

(13)

\[ = \int_0^{\infty} \left[ \Gamma_{\lambda}(t-t') \right]^2 dt'dt + \int_0^{\infty} \left[ \Gamma_{\lambda}(t-t'-\xi)\Gamma_{\lambda}(t-t'+\xi) \right] dt'dt'. \]

For \( T_o \gg \tau_c \), the first term of (13) equals \( T_o^{1/2}\left[\Gamma_{\lambda}(0)\right]^2 \) (Goodman, 2000). The second term reduces to the first for \( \xi = 0 \), and vanishes for \( \xi \gg \tau_c \). Using equations (9), (10) and (13):

\[ \sigma_i^2 = \sigma_{V,\lambda,0}^2(0) + 4\sigma_{V,\lambda,0}^2(\tau) + \sigma_{V,\lambda,0}^2(2\tau) = 7\tau_c T_o \left[\Gamma_{\lambda}(0)\right]^2, \]

(14)

\[ \sigma_o^2 = \tau_c T_o \left[\Gamma_{\lambda}(0)\right]^2. \]

(15)

The Q parameter for UWB communication based on Gaussian noise with TR is given by:

\[ Q_{TR} = \frac{(I_1 - I_0)}{(\sigma_i + \sigma_o) = \sqrt{T_o/\tau_c}/\sqrt{7 + 1} = 0.27 \sqrt{T_o/\tau_c}}. \]

(16)

The corresponding value for direct detection equals:

\[ Q_{dir} = \frac{1}{2\pi} \sqrt{T_o/\tau_c} = 2.58Q_{TR}. \]

(17)
3.3 Experimental demonstration of UWB communication

UWB noise generation based on SBS-ASE and its coherent detection were demonstrated experimentally. Light from a DFB laser was directly modulated by an arbitrary waveform generator (see Fig. 9) (Peled et al., 2010, ©2010 IEEE). The modulating waveform was (Zadok et al., 2007):

\[ i(t) = i_0 - \Delta i \left( t \bmod \frac{T_p}{T_v} \right)^\frac{3}{2}, \quad \text{(18)} \]

where \( T_p = 500 \text{ ns} \) is the modulation period, \( i_0 = 80 \text{ mA} \) is the DFB bias current and \( \Delta i \sim 7.5 \text{ mA} \) is the modulation magnitude. A heterodyne measurement of the modulated DFB PSD is shown in Fig. 10 (top). The DFB output was amplified to 250 mW by an EDFA, and launched into 3.5 km of HNLF (\( \alpha = 1 \text{ dB/km} \)) as an SBS pump wave. Fig. 10 (center) shows the PSD \( \tilde{V}(\Omega) \) of the down-converted SBS-ASE noise. \( \tilde{V}(\Omega) \) is uniform within a range of 1.1 GHz. The arbitrary central frequency of 2.4 GHz was chosen due to equipment limitations. \( \tilde{V}(\Omega) \) can be broadened beyond 10 GHz with stronger pump amplification (Zhu et al., 2007), hence no fundamental limitations prevent the compliance of the noise waveform with the FCC standard. Fig. 10 (bottom) shows a histogram of \( V(t) \), alongside a Gaussian distribution of equal variance. The SBS-ASE noise is well described by Gaussian statistics.

The SBS-ASE optical field was modulated by square waves using an electro-optic modulator. First, the lower arm of the MZI was disconnected, and the modulated noise was directly detected. Fig. 11 (top) shows an example of the detected waveform with \( T_v = 112 \text{ ns} \). \( Q_{\text{dir}} \) was estimated by sampling \( V(t) \) over several hundred periods, and calculating equation (8) with \( \tau = 0 \). The results for \( T_v = 112 \) and 225 ns were \( Q_{\text{dir}} = 10 \) and 14.7, respectively. The results agree with the predicted values of 11.1 and 15.8. The differences could be due to the finite extinction ratio of the modulator and additive detector noise.
Ultra-Wideband Waveform Generation Using Nonlinear Propagation in Optical Fibers

Fig. 10. Top – Power spectral density (PSD) of the directly modulated stimulated Brillouin scattering (SBS) pump wave. Center – PSD of the down-converted SBS amplified spontaneous emission (SBS-ASE) $V(\Omega)$. Bottom - Histogram of the down-converted SBS-ASE noise $V(t)$ (bar), alongside a zero-mean Gaussian distribution of equal variance (line). ©2010 IEEE.

TR-assisted coherent detection of UWB noise communication was demonstrated by reconnecting the lower arm of the MZI with $\tau$ of 12.2 ns. Fig. 11 (center) shows an example of $V_{\text{TR}}(t)$ and the bottom panel shows its autocorrelation. A secondary peak corresponding to $\tau$ is evident. Fig. 12 shows an example of the calculated experimental histograms of $Y^{(1)}[n]$ and $Y^{(0)}[n]$. The estimated $Q_{\text{TR}}$ values for $T_s = 112$ and 225 ns were 3.25 and 4.6, respectively. Based on the experimental values of $Q_{\text{dir}}$, equation (17) suggests a $Q_{\text{TR}}$ of 3.9 and 5.7 for the two symbol durations. The difference may stem from unequal power splitting in the MZI or residual statistical correlation among the terms of $Y^{(1)}[n]$ (see equation (9)).

3.4 UWB noise radar based on SBS-ASE

The SBS-ASE UWB noise waveforms discussed above were also used in a proof-of-concept radar measurement. To that end, the generated waveform $V(t)$ was split in two branches. The waveform in one branch was amplified to -5 dBm and transmitted by a horn antenna with a gain of 20 dBi. The waveform was reflected from a 40X40 cm$^2$ metallic object at different distances. The reflections were collected by a second, identical antenna, amplified and sampled by a real-time digitizing oscilloscope with a bandwidth of 6 GHz. A replica of $V(t)$ in the other arm was sampled by a second oscilloscope channel as a reference. The correlation function between the two sampled waveforms was calculated, and the distance to the target was estimated based on the timing of the observed correlation peak. Figure 13...
shows the measured correlation for several target distances. The full width at half-maximum of the correlation peaks suggests an estimated resolution of 20 cm, in good agreement with the expected value of 15 cm for a 1 GHz-wide noise waveform.

Fig. 11. Top – Measured modulated noise $V(t)$ with no transmitted reference, symbol duration $T_0 = 112$ ns. Center – Measured $V_{TR}(t)$ with a transmitted reference, $T_0 = 112$ ns, relative delay $\tau = 12.2$ ns. Bottom- Normalized autocorrelation of $V_{TR}(t)$ ($T_0, \tau$ as above). ©2010 IEEE.

Fig. 12. Experimental histograms of the decision variable $Y[n]$ for ultra-wideband noise communication with a transmitted reference, based on amplified spontaneous emission from Brillouin scattering. $T_0 = 112$ ns, $\tau = 12.2$ ns Left: logical ‘0’. Right: logical ‘1’. Histograms consist of 160 symbols. ©2010 IEEE.
Ultra-Wideband Waveform Generation Using Nonlinear Propagation in Optical Fibers

Fig. 13. Measured correlation between a UWB noise waveform reflected from a metal target and a reference replica. The transmitted 1 GHz-wide noise waveforms were optically generated using SBS-ASE. The distances to the target were 1.5 m (blue, dotted); 1.95 m (red, solid) and 2.85 m (black, dashed).

4. Concluding remarks

In this chapter, nonlinear propagation over optical fibers was used for the generation of UWB waveforms. Two different nonlinear mechanisms had been employed: SPM and SBS. The generation of both UWB impulse radio shapes and UWB noise had been demonstrated. Impulse radio pulse shapes were generated based on SPM. The technique relied on the time-to-frequency mapping that accompanies SPM spectral broadening of pulses, in implementing all-optical edge detectors. The edge detectors provided temporally-narrowed replicas of an input train of standard pulses. The shapes of the narrow replicas were later electrically subtracted from that of the original pulses by a differential detector. The method provides multiple degrees of freedom for shaping high-order UWB waveforms of high central radio frequencies, up to 34 GHz. Noise waveforms were generated based on the ASE that accompanies SBS in fiber. The ASE noise bandwidth was broadened to 1.1 GHz via pump modulation. The method is readily extendable to the generation of waveforms having arbitrary central radio frequencies, and widths approaching 10 GHz. The noise waveforms were used in proof-of-concept demonstrations of transmit-reference UWB communication and UWB noise radar.

The techniques reported rely on off-the-shelf components only. Few of the components included in the experimental setups, such as EDFA, HNLF or differential detector, are currently too expensive for certain applications. Higher cost may be more tolerable in applications in which a single transmitter is broadcasting to a large number of simple receivers, or where waveforms of high-order and high-frequency are required.
A primary motivation which is driving microwave photonics research in general, and UWB-related photonic techniques in particular, is the potential for a radio-over-fiber integrated system which brings together fiber-optic distribution and broadband all-optical processing. In this respect, techniques which employ the fiber itself as the waveform-generating medium stand out. Future work will be dedicated to advance the proposed methods towards applications.

5. References


Ultra-Wideband Waveform Generation Using Nonlinear Propagation in Optical Fibers


Ultra-Wideband Waveform Generation Using Nonlinear Propagation in Optical Fibers


